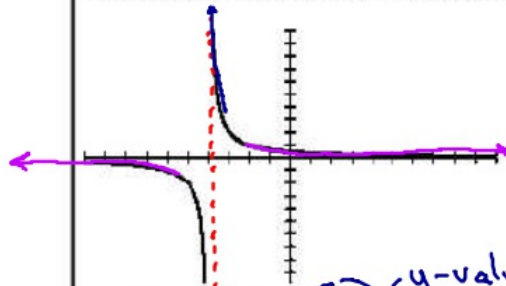


Evaluate the limit based on the graph of f shown



$x = -4$  VA

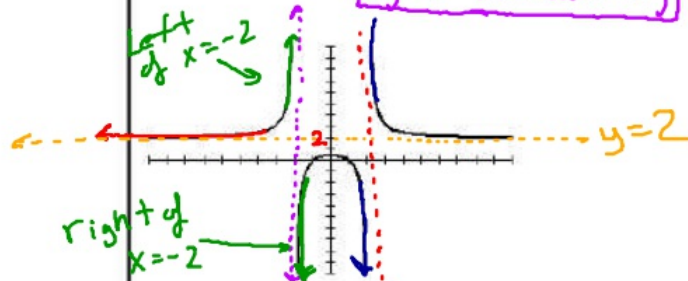
The limits either approach  $+\infty$  or  $-\infty$

a)  $\lim_{x \rightarrow -4^-} f(x) = -\infty$  (y-values)  
 $\lim_{x \rightarrow -4^-} f(x) = -\infty$   
 $x \rightarrow -4^-$  Left

b)  $\lim_{x \rightarrow -4^+} f(x) = \infty$   
 right side of  $x = -4$

c)  $\lim_{x \rightarrow -\infty} f(x) = 0$  ← End Behavior → d)  $\lim_{x \rightarrow \infty} f(x) = 0$   
 $x \rightarrow -\infty$

$y = 0$  Horizontal Asy



a)  $\lim_{x \rightarrow -2^-} f(x) = \infty$

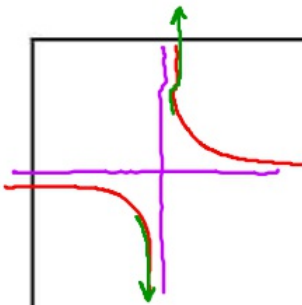
b)  $\lim_{x \rightarrow -2^+} f(x) = -\infty$

c)  $\lim_{x \rightarrow 2^-} f(x) = -\infty$

d)  $\lim_{x \rightarrow 2^+} f(x) = \infty$

e)  $\lim_{x \rightarrow -\infty} f(x) = 2$

f)  $\lim_{x \rightarrow \infty} f(x) = 2$



Find the domain of the function  $f$ . Use limits to describe the behavior of  $f$  at values of  $x$  not in the domain.

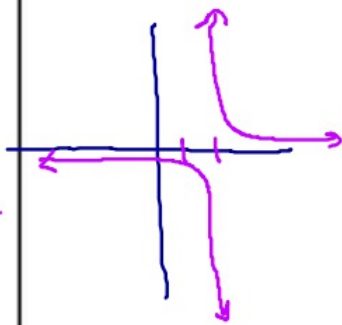
A)  $f(x) = \frac{1}{x}$

$x \neq 0$  - VA

Domain  $(-\infty, 0) \cup (0, \infty)$

$\lim_{x \rightarrow 0^-} f(x) = -\infty$

$\lim_{x \rightarrow 0^+} f(x) = \infty$



B)  $f(x) = \frac{1}{x-2}$

$x-2=0$   
 $x=2$  VA

D:  $(-\infty, 2) \cup (2, \infty)$

$\lim_{x \rightarrow 2^-} f(x) = -\infty$

$\lim_{x \rightarrow 2^+} f(x) = \infty$

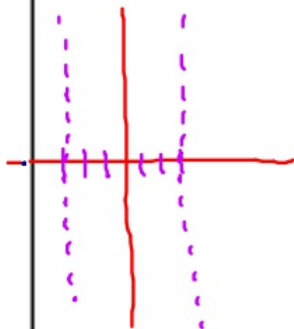
C)  $f(x) = \frac{4}{x^2-9}$

$x^2-9=0$   
 $\sqrt{x^2}=\sqrt{9}$   
 $x=\pm 3$  VA

D:  $(-\infty, -3) \cup (-3, 3) \cup (3, \infty)$

$\lim_{x \rightarrow 3^-} f(x) = -\infty$      $\lim_{x \rightarrow 3^+} f(x) = \infty$

$x=2.9$   $y = \frac{4}{2.9^2-9}$   $y = \frac{4}{\text{neg}}$   
 $x=3.1$   $y = \frac{4}{3.1^2-9}$   $y = \frac{4}{+}$



$\lim_{x \rightarrow -3^-} f(x) = \infty$

$\lim_{x \rightarrow -3^+} f(x) = -\infty$

$x=-3.1$   $f(3.1) = \frac{4}{3.1^2-9}$   
 $y = \frac{4}{+}$   
 $y = +$

$x=-2.9$   $y = \frac{4}{(-2.9)^2-9}$   
 $y = \frac{4}{\text{neg}}$   
 $y = \text{neg}$