

PRE-CALCULUS: by Finney, Demana, Watts and Kennedy
Chapter 2: Polynomial, Power, and Rational Functions 2.4: Real Zeros of Polynomial Functions

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What you'll Learn About

Divide $f(x)$ by $d(x)$ using factoring.

$$1) f(x) = x^2 + 5x + 6 \quad d(x) = x + 2$$

$$\frac{f(x)}{d(x)} = \frac{x^2 + 5x + 6}{x + 2} = \frac{(x+3)(x+2)}{x+2} = x+3$$

$$\frac{75}{3}$$

$$\begin{array}{r} 25 \\ 3 | 75 \ 5 \\ 2(3) \cancel{-6} \\ \underline{15} \\ 15 \\ \hline 5 \\ 3 \\ \hline (2) \\ \text{Remainder} \\ \frac{75}{3} = 251 \frac{2}{3} \end{array}$$

Divide $f(x)$ by $d(x)$ using long division.

$$2) f(x) = x^2 + 5x + 6 \quad d(x) = x + 2$$

$$\begin{array}{r} x+3 \\ x+2 \sqrt{x^2 + 5x + 6} \\ \underline{-x^2 - 2x} \\ x(x+2) \\ \underline{-3x + 6} \\ 3(x+2) \\ \underline{-3x + 6} \\ 0 \end{array}$$

Divide $f(x)$ by $d(x)$ using synthetic division.

$$3) f(x) = x^2 + 5x + 6 \quad d(x) = x + 2$$

$$\begin{array}{l} x+2=0 \\ x=-2 \end{array}$$

$$\begin{array}{r} -2 | 1 \ 5 \ 6 \\ \quad \quad \quad -2 \ -6 \\ \hline \quad \quad \quad 1 \ 3 \ [0] \text{ Remainder} \\ \quad \quad \quad x+3 \end{array}$$

$$\frac{f(x)}{d(x)} = x^2 - \frac{7}{3}x + \frac{38}{9} + \frac{-139/9}{3x+2} \quad \left| \begin{array}{l} x^2 - \frac{7}{3}x + \frac{38}{9} - \frac{139}{9(3x+2)} \end{array} \right.$$

Divide $f(x)$ by $d(x)$ by using long division, and write a summary statement in polynomial form and fraction form.

1) $f(x) = 3x^3 + 5x^2 + 8x + 7 \quad d(x) = 3x + 2$

$$f(x) = 3x^3 - 5x^2 + 8x - 7$$

$$\frac{f(x)}{d(x)}$$

$$\frac{3(\text{what})}{3} = -\frac{7}{3}$$

what = $-\frac{7}{3}$

$$\frac{\left(\frac{38}{3}\right)}{(3)} = \frac{38}{3} \cdot \frac{1}{3}$$

$\downarrow \frac{38}{3} : 3$

$$\begin{array}{r} x^2 - \frac{7}{3}x + \frac{38}{9} \\ 3x+2 \overline{)3x^3 - 5x^2 + 8x - 7} \\ x^2(3x+2) - 3x^3 + 2x^2 \\ \hline -7x^2 + 8x - 7 \\ -7x^2 + \frac{14}{3}x \\ \hline \frac{38}{3}x - 7 \\ -\frac{38}{3}x + \frac{76}{9} \\ \hline -\frac{139}{9} \end{array}$$

Remainder

Divide $f(x)$ by $d(x)$ by using synthetic division, and write a summary statement in polynomial form and fraction form.

2) $f(x) = 3x^3 + 5x^2 + 8x + 7 \quad d(x) = 3x + 2$

Linear

$$3x + 2 = 0 \quad x = -\frac{2}{3}$$

$$\begin{array}{r} -\frac{2}{3} \\ \hline 3 & -5 & 8 & -7 \\ & -2 & +\frac{14}{3} & -\frac{76}{9} \\ \hline 3 & -7 & \frac{38}{3} & -\frac{139}{9} \end{array}$$

$$\frac{3x^2 - 7x + \frac{38}{3}}{3} - \frac{139/9}{3x+2}$$

$$\boxed{x^2 - \frac{7}{3}x + \frac{38}{9} - \frac{139}{9(3x+2)}}$$