

What you'll Learn About

Find the domain of the function algebraically.
 Support your answer graphically

Domain:
 Left to Right
 x-axis
 $x_{min} - x_{max}$

A) $f(x) = x^2 - 9$

All real #'s
 $-\infty \leq x \leq \infty$
 $(-\infty, \infty)$

B) $f(x) = \frac{3}{x} + \frac{7}{x-1}$

$x \neq 0$ $x-1 \neq 0$
 $x \neq 1$

$(-\infty, 0) \cup (0, 1) \cup (1, \infty)$

* Set the denominator = 0
 - These are the x-values that don't work (not in domain)

C) $f(x) = \frac{x}{x^2 + 2x - 3}$

$x^2 + 2x - 3 \neq 0$
 $(x+3)(x-1) \neq 0$
 $x+3 \neq 0$ $x \neq -3$ $x-1 \neq 0$ $x \neq 1$

$(-\infty, -3) \cup (-3, 1) \cup (1, \infty)$

D) $f(x) = \frac{x}{x^2 + 2x}$

$f(x) = \frac{x}{x^2 + 2x}$

$x^2 + 2x \neq 0$
 $x(x+2) \neq 0$
 $x \neq 0$ $x+2 \neq 0$
 $x \neq -2$

$(-\infty, -2) \cup (-2, 0) \cup (0, \infty)$

* You can only sq. root positive numbers and 0.

E) $f(x) = \frac{\sqrt{9-x^2}}{x-5}$

$x-5 \neq 0$
 $x \neq 5$

$9 - x^2 \geq 0$
 $-9 \quad -9$
 $\frac{-x^2 \geq -9}{-1 \quad -1}$
 $\sqrt{x^2} \leq \sqrt{9}$

$x \leq 3$ $x \geq -3$

$[-3, 3]$

$9 - x^2 \geq 0$
 $+x^2 + x^2$
 $\hline 9 \geq x^2$

Domain?

F) $f(x) = \frac{\sqrt{1-x}}{(x+2)(x^2+4)}$

$x+2 \neq 0$ ~~$x^2+4 \neq 0$~~
 $x \neq -2$ ~~$\frac{x^2+4}{x^2+4} \neq 0$~~
 ~~$\sqrt{x^2+4} \neq 0$~~

$1-x \geq 0$
 $+x \quad +x$
 $1 \geq x$
 $(-\infty, 1]$

G) $f(x) = \sqrt{x^3-4x}$

$x^3-4x \geq 0$

$x(x^2-4) \geq 0$

$x \geq 0$ $x^2-4 \geq 0$

$[0, \infty)$ $x^2 \geq 4$

$x \geq 2$ $x \leq -2$

Domain $[2, \infty) \cup (-\infty, -2] \cup x=0$

* If you have
a sq. root
- take what is
underneath the
sq. rt ≥ 0