

Zeros

Graph each function and find the zeros.

$$f(x) = x^3 - 6x^2 + 9x$$

$$g(x) = x^4 - 10x^3 + 32x^2 - 38x + 25$$

$$h(x) = 4x^3 - 9x^2 - 10x + 3$$

$$p(x) = x^3 - 5x^2 - 8x + 12$$

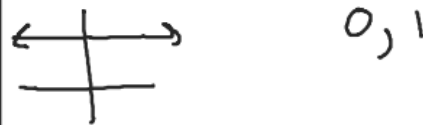
$$f(x) = x^4 - 12x^3 + 19x^2 + 12x - 20$$

$$t(x) = x^4 - 7x^3 + 17x^2 - 17x + 6$$

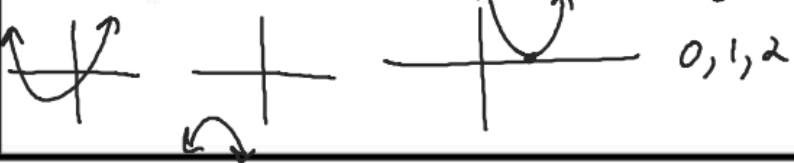
$$y = 4x$$

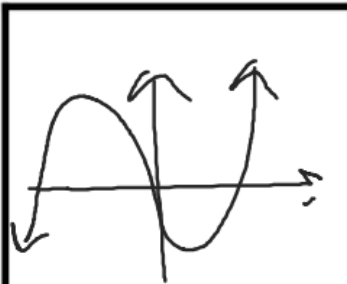


What are the possible number of zeros for a linear function? $D=1$



What are the possible number of zeros for a quadratic function? $D=2$

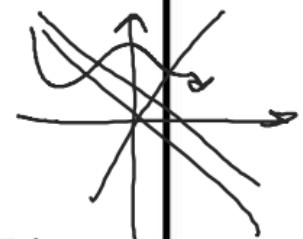




What are the possible number of zeros for a cubic function?

$D=3$

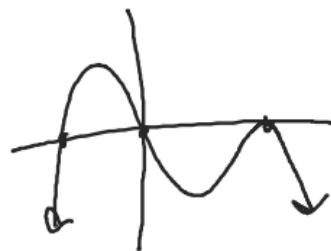
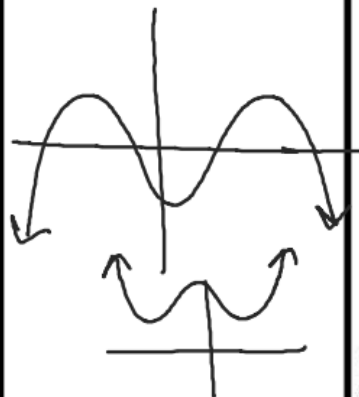
1, 2, 3



What are the possible number of zeros for a quartic function?

$D=4$

0, 1, 2, 3, 4

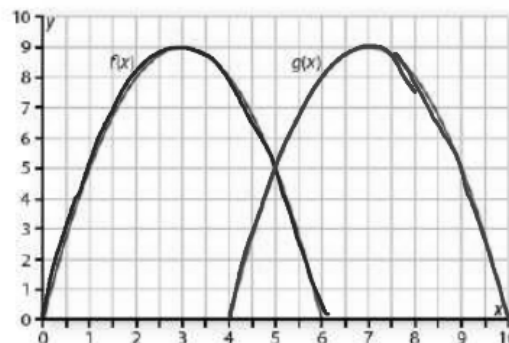


How does the degree of a polynomial seem to be related to the number of zeros of the related polynomial function?

Degree is max # of zeros.

The two parabolas that make up the "m" in the following diagram can be created by graphing $f(x) = -x^2 + 6x$ and $g(x) = -x^2 + 14x - 40$.

Zeros and Products of Polynomials



GCF

Standard Form

$$y = ax^2 + bx + c$$

Factored

$$y = a(x-p)(x-q)$$

FOIL

$$a \cdot b = 0$$

Write each equation in equivalent factored form.

$$f(x) = -x^2 + 6x$$

$$f(x) = -x(x-6)$$

$$g(x) = -x^2 + 14x - 40$$

$$g(x) = -(x^2 - 14x + 40)$$

$$-(x-10)(x-4)$$

Standard Form

Factored Form

For each function write the rule in both standard form and factored form.

$$h(x) = x^2 + 4x$$

$$= x(x+4)$$

$$j(n) = -n^2 + n + 6$$

$$= -(n^2 - n - 6)$$

$$-(n-3)(n+2)$$

$$\frac{-6}{-3 \cdot 2}$$

$$k(x) = (2x-1)(x+5)$$

$$2x^2 + 10x - x - 5$$

$$2x^2 + 9x - 5$$

Using the functions above, show how to use the factored form to find zeros of the function and x-intercepts of its graph.

$$h(x) = x(x+4)$$

$$0 = \overset{a}{x}(\overset{b}{x+4})$$

$$x=0 \quad x+4=0$$

$$x=-4$$

$$k(x) = (2x-1)(x+5)$$

$$2x-1=0 \quad x+5=0$$

$$+1 \quad +1$$

$$2x=1 \quad x=-5$$

$$x=\frac{1}{2}$$

$$j(n) = -(n-3)(n+2)$$

$$0 = -(n-3)(n+2)$$

$$0 = (\overset{a}{n-3})(\overset{b}{n+2})$$

$$n-3=0 \quad n+2=0$$

$$n=3$$

$$n=-2$$

$$-\left(\frac{1}{2}-3\right)\left(\frac{1}{2}+2\right)$$

$$-(-2.5)(2.5)$$

$(-2)^2 + 4(-2)$
 $4 + (-8)$
 -4 zeros $x=0, -4$

 Zeros $x = \frac{1}{2}, -5$
 $(2(-2.25) - 1)(-2.25 + 5)$
 $(-1)(5)$
 $y = ax^2 + bx + c$
 L.O.S. $x = -\frac{b}{2a}$
 max/min $x = -\frac{b}{2a}$
 find y plug $-\frac{b}{2a}$ back into equation
 y-intercept $(0, c)$

Using the same function, use the factored form and information about the x-intercepts to find the line of symmetry, the maximum or minimum point, and the y-intercept of the graph.

$x^2 + 4x$
 $h(x) = x(x+4)$ L.O.S. $x = -2$
 $= 0(0+4)$ min $(-2, -4)$
 $= 0(4)$ y-intercept $(0, 0)$
 $k(x) = (2x-1)(x+5)$ L.O.S. $x = -2.25$
 $(2(0)-1)(0+5)$ min $(-2.25, -5.125)$
 $(-1)(5)$ y-intercept $(0, -5)$

Use the standard form of the polynomial to locate the line of symmetry, maximum or minimum point, and y-intercept of the graph.

$h(x) = x^2 + 4x$ $-\frac{b}{2a} = -\frac{4}{2(4)} = -2$
 $j(n) = -n^2 + n + 6$ $a = -1, b = 1, c = 6$
 $-\left(\frac{1}{2}\right)^2 + \frac{1}{2} + 6 = -\frac{1}{4} + \frac{1}{2} + 6$
 $-\frac{1}{4} + \frac{1}{2} + 6$
 L.O.S. $x = \frac{1}{2}$
 max $\left(\frac{1}{2}, 6\frac{1}{4}\right) \rightarrow (0.5, 6.25)$
 $k(x) = 2x^2 + 9x - 5$ $x = -\frac{b}{2a} = -\frac{9}{2(2)} = -\frac{9}{4}$
 y-intercept $(0, 6)$

zeros $x = 7, -2$
 L.O.S. $x = \frac{1}{2}$
 max $\left(\frac{1}{2}, \frac{25}{4}\right)$
 $(.5, 6.25)$
 y-intercept $(0, 6)$

Consider the function $q(x) = x(x-3)(x+5)$.

- What are the zeros of $q(x)$?
- Write the rule for $q(x)$ in standard form.