

Standard

$$y = ax^2 + bx + c$$

Intercept

$$y = a(x-p)(x-q)$$

Graphing in Vertex Form

$$f(x) = a(x-h)^2 + k$$

Vertex (h, k)

y-intercept
Let $x=0$

Locate the vertex of each quadratic function. Tell whether it is a maximum value or a minimum value. Find the y-intercept for each equation.

$$g(x) = (x-3)^2 + 5$$

Vertex $(3, 5)$

Minimum

$$(0-3)^2 + 5$$

$$(-3)^2 + 5$$

$$9 + 5$$

$(0, 14)$

$$f(x) = -3(x-7)^2 - 12$$

V $(7, -12)$

max

$$-3(0-7)^2 - 12$$

$$-3(-7)^2 - 12$$

$$-3(49) - 12$$

$$-147 - 12 \quad (0, -159)$$

$$m(x) = (x+1)^2 + 25$$

V $(-1, 25)$

min

$$(0+1)^2 + 25$$

$(0, 26)$

$$n(x) = -2(x+6)^2 + 20$$

V $(-6, 20)$

max

$$-2(0+6)^2 + 20$$

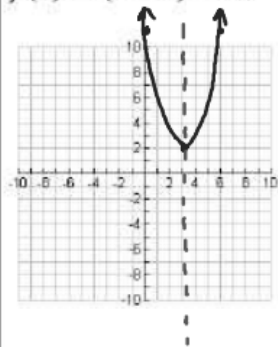
$$-2(6)^2 + 20$$

$$-2(36) + 20$$

$$-72 + 20$$

$$-52$$

$$f(x) = (x-3)^2 + 2$$



Vertex $(3, 2)$

A.O.S $x=3$

y-intercept

$$(0-3)^2 + 2$$

$$(-3)^2 + 2$$

$$9 + 2 = 11$$

D: $(-\infty, \infty)$

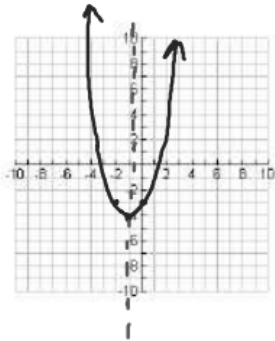
R: $[2, \infty)$

I: $(3, \infty)$

O: $(-\infty, 3)$

$$(x-(-1))^2$$

$$f(x) = (x+1)^2 - 4$$



$$V: (-1, -4)$$

$$A.O.S. x = -1$$

$$y\text{-int } (0, -3)$$

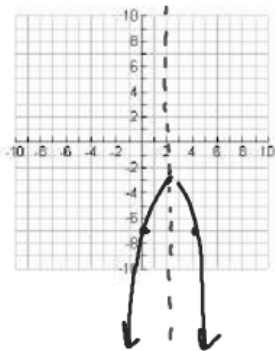
$$D (-\infty, \infty)$$

$$R [-4, \infty)$$

$$Inc (-1, \infty)$$

$$Dec (-\infty, -1)$$

$$f(x) = -(x-2)^2 - 3$$



$$V(2, -3)$$

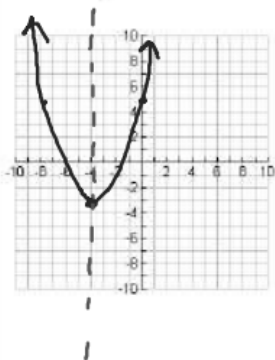
$$-(0-2)^2 - 3$$

$$-(-2)^2 - 3$$

$$-(4) - 3$$

$$-4 - 3 = -7$$

$$f(x) = \frac{1}{2}(x+4)^2 - 3$$



$$V(-4, -3)$$

$$y\text{-int } (0, 5)$$

Standard \rightarrow Intercept

$y = ax^2 + bx + c$ $y = a(x-p)(x-q)$
 Factor

Standard \rightarrow Vertex

$ax^2 + bx + c \rightarrow a(x-h)^2 + k$

Complete the Square

a has to equal 1

Step 1 Divide b term by 2

Step 2 Square answer from step 1

$\left(\frac{15}{2}\right)^2$

Find the value of c that completes the square. Write your expression as a square of a binomial.

$x^2 + 12x + c$
 $x^2 + 12x + 36$
 $(x+6)^2$

$x^2 - 15x + c$
 $x^2 - 15x + \frac{225}{4}$
 $(x - \frac{15}{2})^2$
 $x^2 - \frac{25}{13}x + c$ $\left(\frac{25}{24}\right)^2$

$x^2 - \frac{25}{13}x + \frac{625}{176}$
 $(x - \frac{25}{26})^2$

$x^2 - 6x + c$
 $x^2 - 6x + 9$
 $(x-3)^2$

$x^2 + 11x + c$
 $x^2 + 11x + \frac{121}{4}$
 $(x + \frac{11}{2})^2$

$\left(\frac{11}{2}\right)^2 = \frac{121}{4}$
 $\frac{11}{1}$

Use completing the square to write each function in vertex form. Label the vertex and find the y-intercept.

$f(x) = x^2 - 6x + 11$
 $f(x) - 11 = x^2 - 6x + 9$
 $+9$
 $f(x) - 2 = (x-3)^2$
 $f(x) = (x-3)^2 + 2$
 V(3,2)

$f(x) = x^2 - 2x - 9$
 $f(x) + 9 = x^2 - 2x + 1$
 $+1$
 $f(x) + 10 = (x-1)^2$
 $f(x) = (x-1)^2 - 10$
 V(1,-10)