

Bill and Ted are throwing snowballs into the parking lot from their third story balcony with initial height of 24 feet and upward velocity of 48 feet per second.

Write a function rule that will represent the given scenario for height as a function of time. $(1.5, 60)$

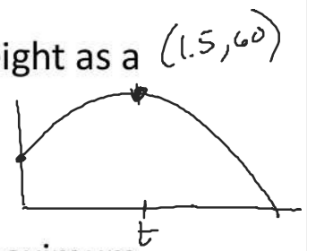
$$h(t) = h_0 + v_0 t - 16t^2$$

$$a = -16$$

$$b = 48$$

$$c = 24$$

$$h(t) = 24 + 48t - 16t^2$$



Without graphing, find the time when the snowball reaches its maximum

height? $t = \frac{-b}{2a} = \frac{-48}{2(-16)} = \frac{-48}{-32} = 1.5 \text{ sec}$

What is the maximum height?

$$\begin{aligned} h(1.5) &= 24 + 48(1.5) - 16(1.5)^2 \\ &= 60 \text{ ft} \end{aligned}$$

Mike owns his own Bungee Jump Business. He has calculated the Income for his company by the following function $I(p) = 50p - p^2$. The following graph shows income as function of price for Mike's business where p is the ticket price and I is the income.

$$I(p) = bx - ax^2 \quad x(b - ax)$$

$$\text{Zeros} = x = 0 \\ x = -\frac{b}{a}$$

Without graphing, find the price of the ticket that will yield a profit of zero dollars?

$$I(p) = p(50 - p)$$

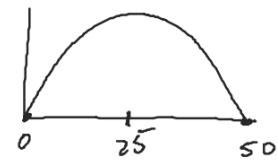
$$\text{price} = \$0, \$50$$

$$p = 0 \quad 50 - p = 0$$

$$50 = p$$

What price should Mike charge to maximize his profit?

$$p = \$25$$



Based on this model what is Mike's maximum profit?

$$I(25) = 50(25) - (25)^2 \\ = \$625$$

Alex hit a baseball 5 feet off the ground. After 5 seconds the ball had a height of 240 feet. Find the initial upward velocity of the baseball. Write an equation for the path of the baseball over time.

$$h(t) = 5 + v_0 t - 16t^2$$

$$\begin{matrix} (5, 240) \\ t & h(t) \end{matrix}$$

$$240 = 5 + v_0(5) - 16(5)^2$$

$$240 = 5 + v_0(5) - 400$$

$$240 = v_0(5) - 395$$

$$\frac{635}{5} = \frac{v_0(5)}{5}$$

$$h(t) = 5 + 127t - 16t^2$$

$$v_0 = 127$$

Without using graphing technology, sketch the pattern of graphs you would expect for the next set of quadratics functions. Justify your reasoning.

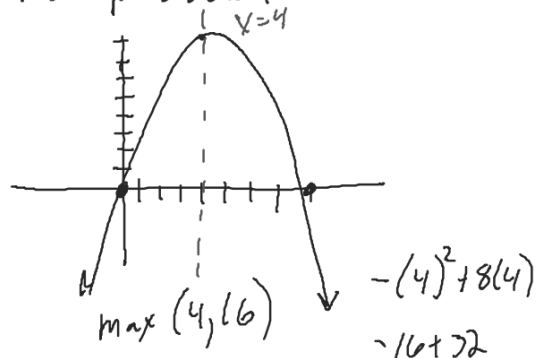
$$y = -x^2 + 8x$$

y-intercept @ zero

x-intercept @ $x=0$

$$x = \frac{-b}{a} = \frac{-8}{-1} = 8$$

$a < 0$ opens down



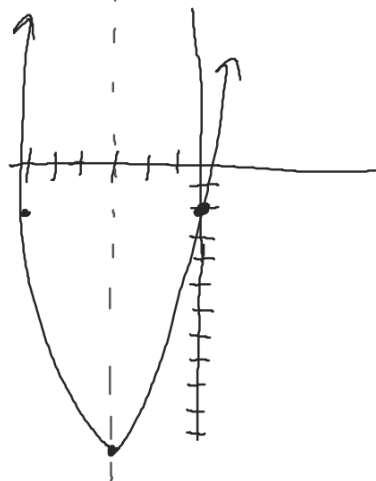
$$y = x^2 + 6x - 2$$

y-intercept @ $y = -2$

open up $a > 0$

Shift left

$$\begin{aligned} \text{min} \rightarrow x &= \frac{-b}{2a} \\ &= \frac{-6}{2(1)} \\ &= -3 \end{aligned}$$



$$\begin{aligned} &(-3)^2 + 6(-3) - 2 \\ &9 - 18 - 2 \\ &-9 - 2 \\ &-11 \end{aligned}$$

Match the equation to the graph and be prepared to explain your answer.

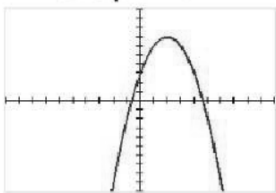
Rule I $y = x^2 - 4x$

Rule II $y = x^2 + 3x - 1$

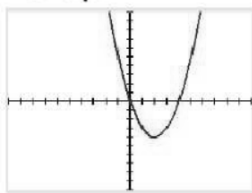
Rule III $y = -x^2 + 4x + 3$

Rule IV $y = -4x^2 + 2x + 3$

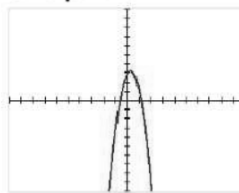
Graph A



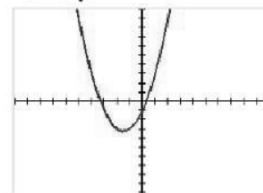
Graph B



Graph C



Graph D



Rule $y = -x^2 + 4x + 3$

Rule $y = x^2 - 4x$

Rule $y = -4x^2 + 2x + 3$

Rule $y = x^2 + 3x - 1$

Explain

$a < 0$ opens down
y-intercept of 3

Explain $a > 0$ opens up
y-intercept of zero
x-intercepts zero
 $x = 4$

Explain

$a < 0$ opens down
y-intercept of 3
 $a = 4$ Skinnier

Explain $a > 0$ open up
y-intercept -1

For each function, explain what you can learn about the shape and location of its graph by looking at the coefficients and constant term in the rule.

$$h = 15 - 16t^2$$

$$h = 2 + 40t - 16t^2$$

$$h = 0.004x^2 - x + 80$$

$$h = 0.05s^2 + 1.1s$$